

## Presenter's Notes

### Fermi Problems

#### Principles to Actions: Effective Mathematics Teaching Practices

Slide 1	Facilitator should welcome participants and introduce him/herself to the audience.
Slide 2	<p><a href="https://www.freeimages.com/search/that-me/3">https://www.freeimages.com/search/that-me/3</a></p> <p>Warm-up Activity: Ask participants to stand if:</p> <ul style="list-style-type: none"><li>• <b>If you love (summer, winter, spring, fall - select current season)</b></li><li>• <b>If you love mathematics</b></li><li>• <b>If you love teaching students</b></li></ul> <p><b>If you are standing – this workshop is for YOU!</b></p> <p>Share with participants that this session will provide valuable insights for all – regardless of assigned grade level assignment!</p>
Slide 3	<p>Source: NCTM <a href="http://www.nctm.org">www.nctm.org</a></p> <p>Review what has happened in the reform of mathematics education in the US:</p> <ul style="list-style-type: none"><li>• <b>1989: Curriculum and Evaluation Standards for School Mathematics</b></li></ul> <p>In 1989, the National Council of Teachers of Mathematics (NCTM) released a document of major importance for improving the quality of mathematics education in grades K-12. This document, "Curriculum and Evaluation Standards for School Mathematics," contains a set of standards for judging mathematics curricula and for evaluating the quality of the curriculum and student achievement. It represents the consensus of NCTM's members about the fundamental content that should be included in the school mathematics curriculum, establishing a framework to guide reform in school mathematics. Inherent in the STANDARDS is the belief that all students need to learn more, and often different, mathematics.</p> <ul style="list-style-type: none"><li>• <b>2000 Principles and Standards for School</b></li></ul> <p>A comprehensive and coherent set of mathematics standards for each and every student from prekindergarten through grade 12, <i>Principles and Standards</i> is the first set of rigorous, college and career readiness standards for the 21st century. <i>Principles and Standards for School Mathematics</i> outlines the essential components of a high-quality school mathematics program. It</p>

	<p>emphasizes the need for well-prepared and well-supported teachers and administrators, and it acknowledges the importance of a carefully organized system for assessing students’ learning and a program’s effectiveness. <i>Principles and Standards</i> calls for all partners—students, teachers, administrators, community leaders, and parents—to contribute to building a high-quality mathematics program for each and every student.</p> <ul style="list-style-type: none"> <li>• <b>2006 Curriculum Focal Points</b></li> </ul> <p>Curriculum Focal Points are the most important mathematical topics for each grade level. They comprise related ideas, concepts, skills, and procedures that form the foundation for understanding and using mathematics and lasting learning. Curriculum Focal Points have been integral in the revision of many state math standards for Pre-K through grade 8.</p> <ul style="list-style-type: none"> <li>• <b>2010 Focus in High School Mathematics</b></li> </ul> <p>Focus in High School Mathematics: Reasoning and Sense Making is a conceptual framework to guide the development of future publications and tools related to grades 9–12 mathematics curriculum and instruction. It suggests practical changes to the high school mathematics curriculum to refocus learning on reasoning and sense making. This shift constitutes a substantial rethinking of the high school math curriculum, advocating for more and better mathematics.</p>
Slide 4	<p>Source: NCTM <i>Principles to Actions</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)</p> <p>Continuing its tradition of mathematics education leadership, NCTM has defined and described the principles and actions, including specific teaching practices, that are essential for a high-quality mathematics education for all students.</p>
Slide 5	<p>The development of the standards began with research-based learning progressions detailing what is known today about how students’ mathematical knowledge, skill, and understanding develop over time. The knowledge and skills students need to be prepared for mathematics in college, career, and life are woven throughout the mathematics standards. However, the Standards do not describe or prescribe the teacher practices or actions that will ensure all students will be successful and mathematically literate.</p>

<p>Slide 6</p>	<p>Standards have contributed to higher achievement, but challenges remain.</p> <ul style="list-style-type: none"> <li>• In 2019, the National Assessment of Educational Progress (NAEP) mathematics assessment was administered to representative samples of fourth- and eighth-grade students in the nation, states, the District of Columbia, Department of Defense schools, and 27 participating large urban districts. The assessment was delivered on digital devices and assessed students' knowledge and skills in mathematics and their ability to solve problems in mathematical and real-world contexts. Students also answered survey questions asking about their opportunities to learn about and engage in mathematics inside and outside of school.</li> <li>• Mathematical performance, for PISA, measures the mathematical literacy of a 15-year-old student to formulate, employ and interpret mathematics in a variety of contexts to describe, predict and explain phenomena, recognizing the role that mathematics plays in the world. The mean score is the measure. A mathematically literate student recognizes the role that mathematics plays in the world in order to make well-founded judgments and decisions needed by constructive, engaged and reflective citizens.</li> <li>• 2019 NAEP: Lower-, middle-, and higher-performing students at grades 4 and 8 made gains compared to the early 1990s and 2000; <b>no significant progress was made at both grades for lower-performing students compared to a decade ago.</b></li> </ul>
<p>Slide 7</p>	<p>Source: NCTM <i>Principles to Actions</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)  Source: NCTM (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)  Summarize the Teaching and Learning Principle, noting the strong emphasis on promoting students' ability to make sense of mathematical ideas and to reason mathematically. Ask the participants to keep this Principle in mind throughout the session and in particular, as they watch the WV Classroom Video.</p>
<p>Slide 8</p>	<p><b>Prior to the workshop</b> and based on the expected number of participants, prepare packets of the Beliefs About Teaching and Learning Mathematics cards. Cut the cards apart, shuffle the cards and place them in an envelope. Each pair or group of participants will need one packet of cards. Also, prepare a packet of cards for you to use during the discussion of the activity.</p>

	<p>During the activity, circulate among the pairs or groups of participants as they work to sort the belief cards.</p> <p>After all pairs or groups have completed the sorting task, ask the participants if there were any belief cards they found difficult to classify as either Productive or Unproductive. Ask why they found it difficult to assign the belief card to a category.</p> <p>Select a belief card from your packet and read the card to the participants. Ask the participants how they classified the belief and why. Repeat selecting cards and engaging the participants until 3 to 5 cards have been discussed. Be sure to select both Productive and Unproductive beliefs.</p> <p>At the end of the discussion, move to the next slide so that participants may see the correct sorting.</p> <p>Source: <i>Principles to Actions, Ensuring Mathematical Success for All</i>, (NCTM, 2014) pg. 11.</p>
Slide 9	Source: <i>Principles to Actions, Ensuring Mathematical Success for All</i> , (NCTM, 2014) pg. 11.
Slide 10	Source: NCTM <i>Principles to Action</i> ( <a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a> )
Slide 11	<p>Source: NCTM <i>Principles to Actions</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)</p> <p>These are the practices at the heart of the work of teaching. According to the research of D. Ball and F.M. Forzani they are the practices that are most likely to affect student learning. Give participants a few minutes to review the list of the eight, research-based, Mathematics Teaching Practices identified by NCTM as highly effective for student learning of mathematics.</p> <p>Ask the participants to identify the most significant noun within each of the eight practices.</p> <ol style="list-style-type: none"> <li>1. Establish mathematics <b>goals</b> to focus learning.</li> <li>2. Implement <b>tasks</b> that promote reasoning and problem solving.</li> <li>3. Use and connect mathematical <b>representations</b></li> <li>4. Facilitate meaningful mathematical <b>discourse</b>.</li> <li>5. Pose purposeful <b>questions</b>.</li> <li>6. Build procedural <b>fluency</b> from conceptual understanding.</li> <li>7. Support productive <b>struggle</b> in learning mathematics.</li> <li>8. Elicit and use <b>evidence</b> of student thinking.</li> </ol>

Slide 12	<p>Source: Creating a Road Map, Corwin Publishing  <a href="https://us.corwin.com/sites/default/files/upm-binaries/92312_Chapter_2_Implementing_Effective_Teaching.pdf">https://us.corwin.com/sites/default/files/upm-binaries/92312_Chapter_2_Implementing_Effective_Teaching.pdf</a></p> <p>Give each participant the handout, Effective Teaching Look Fors.  Discuss the “Look Fors” for each Teaching Practice. Make sure all participants have the same understanding of what each “Look For” as they will be using this “Look Fors” later in the presentation to evaluate teaching methods.</p>
Slide 13	<p>Explain to the participants that they are about to view a video featuring a WV teacher and her students.  Describe the Fermi Problems math activity (See description on screen.)  This lesson should be a culminating activity in a unit on ratio and ratio reasoning.</p>
Slide 14	<p>Explain that this lesson highlights a WV Teacher, Rachel Moon, and her students working with Fermi problems.  The activity in our video, Fermi Problems, is designed for small groups or pairs of students to strengthen their conceptual understanding for ratios and ratio reasoning to solve an unfamiliar, Fermi-style problem Explain that a Fermi problem is an estimation problem designed to teach approximation of extreme calculations.</p> <p>The introduction of the lesson is one of the most crucial parts to engage the students in the math learning time.  No Video Clip</p>
Slide 15	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 12.  One of the research-based, teaching practices identified by NCTM is the importance of establishing clear mathematics goals to focus student learning and to guide teacher decisions. The mathematical purpose of a lesson should not be a mystery to students. Classrooms in which students understand the learning expectations for their work perform at higher levels than classrooms where the expectations are unclear (Haystead and Marzano 2009; Hattie 2009). Although daily goals need not be posted, it is important that students understand the mathematical purpose of a lesson and how the activities</p>

	<p>contribute to and support their mathematics learning. Goals or essential questions motivate learning when students perceive the goals as challenging but attainable (Marzano 2003; McTighe and Wiggins 2013). Teachers can discuss student-friendly versions of the mathematics goals as appropriate during the lesson so that students see value in and understand the purpose of their work (Black and William 1998a; Marzano 2009). When teachers refer to the goals during instruction, students become more focused and better able to perform self-assessment and monitor their own learning (Clarke, Timperley, and Hattie 2004; Zimmerman 2001).</p>
Slide 16	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 12.</p>
Slide 17	<p>Source: YouTube  <a href="https://www.youtube.com/watch?v=EcZBUFqFLxc">https://www.youtube.com/watch?v=EcZBUFqFLxc</a></p>
Slide 18	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 16.</p> <p>Compare the actions of teachers versus the actions of students when establishing mathematics goals to focus learning.</p> <p>Ask the participants if they believe the teacher actions above are routine in their schools. If yes, ask how they know. If no, ask what is needed for the teacher actions above to become routine in their school.</p>
Slide 19	<p>This WV CCRS is one of three standards in the 6<sup>th</sup> grade Ratios and Proportional Relationships cluster.</p>
Slide 20	<p>Read slide to participants.</p>
Slide 21	<p>THINK, PAIR AND SHARE</p> <p>Ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p> <p>Bring the groups back together to share their thoughts.</p>
Slide 22	<p>Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving such as this</p>

	<p>learning activity. Effective teaching with this kind of mathematical problem engages students in solving and discussing real world applications of the math concepts. In this video, Rachel Moon, the teacher is encouraging the students to reason and promote use of the students' prior knowledge to apply this thinking in this task.</p> <p>Video #1 JA 3 0:00-1:30</p>
Slide 23	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 17.</p> <p>There is <b>no decision that teachers make that has a greater impact on students' opportunities to learn and on their perceptions about what mathematics is than the selection or creation of the tasks</b> with which the teacher engages students in studying mathematics.</p> <p>Tasks should provide opportunities for students to think and make sense of mathematics.</p> <p>Having <b>multiple entry points is very important</b> because of the <b>impact on equity</b>. If students can make a table, create a drawing, or use manipulatives, the math becomes more accessible to students who might not immediately know how to solve the problem.</p>
Slide 24	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 17.</p> <p>Tasks should provide opportunities for students to make sense of mathematics. Rich mathematical tasks engage students in sense-making through deeper learning that require high levels of thinking, reasoning, and problem solving.</p>
Slide 25	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 18.</p> <p>THINK, PAIR AND SHARE:</p> <p>Ask participants if the math tasks provided in students' texts have all the characteristics of a GOOD math task. If NO, discuss what traits are usually missing in textbook provided math tasks.</p>

	Ask participants to share how they find GOOD math tasks (outside of the adopted textbook) for their students.
Slide 26	<p>Insert Clip: JA! 0:08 – 6:53</p> <p>Listen as the teacher engages students in this task that will promote mathematical reasoning and problem solving. Think about how you would solve the problem. How do the students react to the problem? Notice what the teacher does and what the students do. Consider its multiple entry points and possible solution strategies and notice how the teacher encourages this. THINK, PAIR AND SHARE Ask participants to respond to the question. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 27	
Slide 28	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 24</p> <p>Ask participants what is meant by representations of mathematical ideas.</p>
Slide 29	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 24</p>
Slide 30	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 25</p> <p>Engage participants in a discussion of the graphic. Some probing questions you might ask include:</p> <ul style="list-style-type: none"> <li>• What is the distinction between physical and visual representations? <ul style="list-style-type: none"> <li>• Describe some physical representations that might support students' thinking.</li> <li>• Describe some visual representations you would expect students to produce.</li> <li>• In the diagram, why do the arrows go both ways?</li> </ul> </li> </ul>



	<p>The point is not for students to use different representations just for the sake of it. What’s crucial is that students are using/connecting representations as TOOLS to solve problems and to build understanding of concepts. The depth of understanding is related to the strength of connections among mathematical representations that students have internalized (Pape and Tchoshanov 2001; Webb, Boswinkel, and Dekker 2008). For example, students develop understanding of the meaning of the fraction <math>\frac{7}{4}</math> (symbolic form) when they can see it as the quantity formed by “7 parts of size one-fourth” with a tape diagram or on a number line (visual form), or measure a string that has a length of 7-fourths yards (physical form).</p>
Slide 31	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 25</p>
Slide 32	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources  <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a>  Provide participants with a copy of the Rich Mathematical Task Rubric. Allow time for participants to read the rubric.  Discuss the Task Levels and the Descriptions for <b>Representations and Connections</b>.</p>
Slide 33	<p>THINK, PAIR AND SHARE  In pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 34	<p>Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving such as this learning activity. Effective teaching with this kind of mathematical problem engages students in solving and discussing real world applications of the math concepts. In this video, Rachel Moon, the teacher is encouraging the students to reason and promote use of the students’ prior knowledge to apply this thinking in this task.</p>
Slide 35	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 29</p>

	Ask participants what their concerns are about facilitating meaningful mathematical discourse.
Slide 36	<p>Source: <i>Asking Questions and Promoting Discourse</i>, NCTM  <a href="https://www.nctm.org/Conferences-and-Professional-Development/Tips-for-Teachers/Asking-Questions-and-Promoting-Discourse/">https://www.nctm.org/Conferences-and-Professional-Development/Tips-for-Teachers/Asking-Questions-and-Promoting-Discourse/</a></p> <p>Mathematical discourse is a powerful sense-making tool, but it doesn't just <i>happen</i>. Students must develop both the inclination and habit of attending to each other's mathematical ideas, and they must have the time and space to make sense of, critique, and develop the ideas. Teacher talk moves are crucial supports for developing students' capacity to engage in productive mathematical discussions (Kazemi and Hintz, 2014; Chapin, O'Connor, and Anderson, 2009).</p>
Slide 37	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p.35.</p> <p>Ask participants about student interest in engaging in mathematical discourse. Why do some students try to avoid participating in mathematical discourse? How can the teacher help students to become more active participants in mathematical discourse?</p>
Slide 38	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources  Grades 6-8 Institute PowerPoint  <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a></p> <p>The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement.</p> <p>Classroom discussion has an effect size of 0.82, which is more than twice what we need to know that a specific strategy will make a difference in learning. Classroom discussion is defined as "a method of teaching that involves the entire class in a discussion.</p> <p>Classroom discussion is a critical area with a huge effect size. Classroom discussions provide the opportunity for students to communicate with one another for a variety of functions including to activate prior knowledge, to</p>

	<p>explore new topics, to learn from others, and to demonstrate their learning. This is an engagement strategy which provides all students the chance to participate, especially when structured in a way that extends beyond a teacher-student question and answer sequence.</p> <p>Consider what <a href="http://visiblelearning.org">visiblelearning.org</a>, asserts regarding what the most effective classrooms discussions should include:</p> <ul style="list-style-type: none"> <li>• creating a series of questions for the students to think about</li> <li>• allocating enough time in the lesson for an elaborate discussion</li> <li>• making sure that students can freely express their opinion without being laughed at or ridiculed</li> </ul>
<p>Slide 39</p>	<p>There is no clip for this slide.</p> <p>THINK, PAIR AND SHARE</p> <p>In pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
<p>Slide 40</p>	<p>Insert clip</p> <p>JA2</p> <p>Splice if possible.</p> <p>11:27 – 12:24</p> <p>21:00 – 23:10</p> <p>Note the way the teacher uses questions to draw information from the students and to help them clarify and organize their thinking.</p>
<p>Slide 41</p>	<p>Ask participants how posing purposeful questions can be used to inform instruction and assess student understanding?</p> <p>Ask participants how posing purposeful questions can promote equitable learning opportunities for all students?</p> <p><b>Identify, in advance, the big ideas that your lesson examines and the mathematical outcomes that students should achieve.</b> Take time to brainstorm the multiple approaches that could be taken to work through similar problems and the misconceptions that students might have. Make sure that you prepare questions that address these multiple approaches and misconceptions, prompting a discussion about when particular approaches are better than others and how to explain why each misconception is faulty. Close each lesson with a summarizing question that reiterates the big ideas.</p>

<p>Slide 42</p>	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM, 2014</p> <p>Effective mathematics teaching relies on questions that encourage students to explain and reflect on their thinking as an essential component of meaningful mathematical discourse. Purposeful questions allow teachers to discern what students know and adapt lessons to meet varied levels of understanding, help students make important mathematical connections, and support students in posing their own questions. However, merely asking questions is not enough to ensure that students make sense of mathematics and advance their reasoning.</p>
<p>Slide 43</p>	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources Grades 6-8 Institute PowerPoint <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a></p> <p>The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement.</p> <p>Ask participants why Self-verbalization and Self-questioning have a greater impact on student achievement.</p> <p>So much of classroom time is spent with teachers questioning the students. Cotton (1989), for example, reviewed the evidence and found questioning was the second most dominant teaching method (after teacher talk), with teachers spending between 35–50 percent of teaching time posing questioning (e.g., Long &amp; Sato, 1983; van Lier, 1998)— that is about 100 questions per hour (Mohr, 1998)—and the responses from the teacher to the students’ answers to these questions was some form of judgment or correction, primarily reinforcing in nature, affirming, restating, and consolidating student responses. Brualdi (1998) claimed that teachers asked 300 to 400 questions per day, and the majority of these were low-level cognitive questions—60 percent recall facts and 20 percent are procedural in nature (Wilén, 1991) These are not open, inquiry questions, as students understand that the teacher already knows the answer (they are “display” questions; 82 percent are of this nature: Cotton, 1989). The reason for so much questioning relates to the conceptions</p>

	<p>of teaching and learning held by many teachers—that is, their role is to impart knowledge and information about a subject, and student learning is the acquisition of this information through processes of repetition, memorization, and recall: hence the need for much questioning to check that they have recalled this information. The overall effects of questioning vary, and the major moderator is the type of question asked—surface questions can enhance surface knowing and higher-order questions can enhance deeper understanding.</p>
<p>Slide 44</p>	<p>Adapted from Smith, M. S., et al. (2017). <i>Taking Action: Implementing Effective Mathematics Teaching Practices</i>, National Council of Teachers of Mathematics, p.102</p> <p>Researchers have created a variety of frameworks to categorize the types of questions that teachers ask (e.g., Boaler and Brodie 2004; Chapin and O’Connor 2007). Though the categories differ across frameworks, commonalities exist among the types of questions. For example, the frameworks generally include questions that ask students to recall information, as well as questions that ask students to explain their reasoning. The chart above displays a set of question types that synthesizes key aspects of these frameworks that are particularly important for mathematics teaching. Although the question types differ with respect to the level of thinking required in a response, all of the question types are necessary in the interactions among teachers and students. For example, questions that gather information are needed to establish what students know, while questions that encourage reflection and justification are essential to reveal student reasoning.</p>
<p>Slide 45</p>	<p>THINK, PAIR AND SHARE</p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
<p>Slide 46</p>	<p>Rachel Moon is teaching that struggling is part of learning math. She wants to encourage creativity and build authentic engagement and perseverance in her students.</p> <p>There is no video for this section.</p>

Slide 47	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014</p> <p>Ask participants to share their thoughts on the importance of fluency with procedures to student success in mathematics.</p> <p>Discuss with the participants the significance of the quote: <i>A rush to fluency undermines students' confidence and interest in mathematics and is considered a cause of mathematics anxiety.</i></p>
Slide 48	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014</p> <p>Paraphrase the bullets on the slide.</p> <p>Fluency is not intended as the main or sole target of instruction. Problem Solving and Reasoning that are the focus of the second teaching practice need to co-exist with procedural fluency. This occurs when students first have opportunities to develop conceptual understanding.</p> <p>Computational fluency is strongly related to number sense and involves so much more than the conventional view of it encompasses. Developing students' computational fluency extends far beyond having students memorize facts or a series of steps unconnected to understanding (Baroody 2006; Griffin 2005)</p> <p>Early work with reasoning strategies is related to algebraic reasoning. As students learn how quantities can be taken apart and put back together in different ways (i.e., decomposition and composition of numbers), they establish a basis for understanding properties of the operations. Students need this early foundation for meaningful learning of more formal algebraic concepts and procedures throughout elementary school and into middle and high school.</p>
Slide 49	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 42.</p> <p>Discuss why is it important to build procedures from conceptual understanding.</p> <p>Ask participants: What kind of "bizarre results" could happen if students are taught mechanical execution of procedures without understanding the mathematical basis?</p>

	<p>Fluency is not a simple idea. Being fluent means that students are able to choose flexibly among methods and strategies to solve contextual and mathematical problems, they understand and are able to explain their approaches, and they are able to produce accurate answers efficiently. Fluency builds from initial exploration and discussion of number concepts to using informal reasoning strategies based on meanings and properties of the operations to the eventual use of general methods as tools in solving problems. This sequence is beneficial whether students are building toward fluency with single- and multi-digit computation with whole numbers or fluency with, for example, fraction operations, proportional relationships, measurement formulas, or algebraic procedures.</p>
Slide 50	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 47</p> <p>Ask participants:          What visual models have they used to build procedural fluency?          Is it important for students to be able to explain why the procedures they used worked? Why?</p>
Slide 51	<p>THINK, PAIR AND SHARE</p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 52	
Slide 53	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014</p> <p>Discuss with the participants the importance for students to be able to figure things out for themselves.</p> <p>It is through this process of figuring things out on their own that they will develop authority and ownership of their own learning.</p>
Slide 54	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p.48.</p>

In comparisons of mathematics teaching in the United States and in high-achieving countries, U.S. mathematics instruction has been characterized as rarely asking students to think and reason with or about mathematical ideas (Banilower et al. 2006; Hiebert and Stigler 2004). Teachers sometimes perceive student frustration or lack of immediate success as indicators that they have somehow failed their students. As a result, they jump in to “rescue” students by breaking down the task and guiding students step by step through the difficulties. Although well intentioned, such “rescuing” undermines the efforts of students, lowers the cognitive demand of the task, and deprives students of opportunities to engage fully in making sense of the mathematics.

Slide  
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Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources  
Grades 6-8 Institute PowerPoint  
[http://www.doe.virginia.gov/instruction/mathematics/professional\\_development/institutes/2019/index.shtml](http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml)

The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement.

There is a high relationship between engagement and degree of concentration on tasks. One way of enhancing concentration is to mentally visualize the processes and strategies involved in a task. Students who mentally visualized various motor tasks were more effective compared to those that did not ( $d = 0.48$ ).

Teachers greatly influence how students perceive and approach struggle in the mathematics classroom. Even young students can learn to value struggle as an expected and natural part of learning, as demonstrated by the class motto of one first-grade math class: “If you are not struggling, you are not learning” (Carter 2008, p. 136). Teachers must accept that struggle is important to students’ learning of mathematics, convey this message to students, and provide time for them to try to work through their uncertainties.

Unfortunately, this may not be enough, since some students will still simply shut down in the face of frustration, proclaim “I don’t know,” and give up. Dweck (2006) has shown that students with a fixed mindset— that is, those who believe that intelligence (especially math ability) is an innate trait—are



	<p>more likely to give up when they encounter difficulties because they believe that learning mathematics should come naturally. By contrast, students with a growth mindset—that is, those who believe that intelligence can be developed through effort—are likely to persevere through a struggle because they see challenging work as an opportunity to learn and grow.</p>
Slide 56	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p.52.</p> <p>Use the chart to engage participants in a discussion of how they support students to persevere in problem solving.</p>
Slide 57	<p>Insert Clip JA2 16:25 – 20:45</p> <p>Watch and listen as the students and teacher work together to make sense of a problem.</p> <p>What evidence is there of productive struggle? What is the teacher doing?</p> <p>THINK, PAIR AND SHARE</p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 58	<p>Set up: In this clip, you will see Rachel Moon eliciting and using evidence of the students' thinking about the activity.</p> <p>Play: Video 2 The times of this clip are 8:30-10:30.</p> <p>Follow-up:</p> <p>What did you notice about the teacher's conversation with the students? Rachel Moon, the teacher, was asking good questions to generate the types of thinking and discussion that are central to the learning goal. She is listening carefully to student thinking and make note of which students need reteaching and note the students who are progressing successfully. When you, the teacher, are eliciting and using evidence of student thinking, some questions you might use are: Who Disagrees? Who will explain why or why not? Who has the same answer, but a different way to explain it? Who has a different answer?</p>

	You, the teacher, are listening carefully to students' ideas during the math learning activity as this task, Fermi problems provides.
Slide 59	Source: <i>Principles to Action: Ensuring Mathematical Success for All</i> , NCTM, 2014, p. 53 Ask participants: What can serve as evidence of student thinking when assessing progress toward understanding? How should the evidence affect what a teacher does instructionally for students?
Slide 60	Source: <i>Principles to Action: Ensuring Mathematical Success for All</i> , NCTM, 2014, p. 53 Ask participants: What is formative assessment? Is it possible to do formative assessment every day? If so, how?
Slide 61	Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources Grades 6-8 Institute PowerPoint <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a> The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement. Cognitive task analysis was among the highest scoring actions to affect student achievement. Ask participants to give an example of what a cognitive task might look like in the classroom and why it is so effective.
Slide 62	THINK, PAIR AND SHARE

	With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.
Slide 63	<p><b>THINK, PAIR AND SHARE – CLOSURE ACTIVITY</b></p> <p>With participants grouped in pairs, ask participants to reflect on what they have learned about the eight Effective Mathematics Teaching Practices. Ask each participant to select 1-2 Practices to study and to implement with students.</p> <p>In pairs, develop a list of actions they will need to take in the pursuit of mathematical success for all their students.</p>
Slide 64	