

## Presenter's Notes

### Fitting Boxes into Boxes

#### Principles to Actions: Effective Mathematics Teaching Practices

Slide 1	Facilitator should welcome participants and introduce him/herself to the audience.
Slide 2	<p><a href="https://www.freeimages.com/search/that-me/3">https://www.freeimages.com/search/that-me/3</a></p> <p>Warm-up Activity: Ask participants to stand if:</p> <ul style="list-style-type: none"><li>• <b>If you love (summer, winter, spring, fall - select current season)</b></li><li>• <b>If you love mathematics</b></li><li>• <b>If you love teaching students</b></li></ul> <p><b>If you are standing – this workshop is for YOU!</b></p> <p>Share with participants that this session will provide valuable insights for all – regardless of assigned grade level assignment!</p>
Slide 3	<p>Source: NCTM <a href="http://www.nctm.org">www.nctm.org</a></p> <p>Review what has happened in the reform of mathematics education in the US:</p> <ul style="list-style-type: none"><li>• <b>1989: Curriculum and Evaluation Standards for School Mathematics</b> In 1989, the National Council of Teachers of Mathematics (NCTM) released a document of major importance for improving the quality of mathematics education in grades K-12. This document, "Curriculum and Evaluation Standards for School Mathematics," contains a set of standards for judging mathematics curricula and for evaluating the quality of the curriculum and student achievement. It represents the consensus of NCTM's members about the fundamental content that should be included in the school mathematics curriculum, establishing a framework to guide reform in school mathematics. Inherent in the STANDARDS is the belief that all students need to learn more, and often different, mathematics.</li><li>• <b>2000 Principles and Standards for School Mathematics</b> A comprehensive and coherent set of mathematics standards for each and every student from prekindergarten through grade 12, <i>Principles and Standards</i> is the first set of rigorous, college and career readiness standards for the 21st century. <i>Principles and Standards for School Mathematics</i> outlines the essential components of a high-quality school mathematics program. It</li></ul>

	<p>emphasizes the need for well-prepared and well-supported teachers and administrators, and it acknowledges the importance of a carefully organized system for assessing students’ learning and a program’s effectiveness. <i>Principles and Standards</i> calls for all partners—students, teachers, administrators, community leaders, and parents—to contribute to building a high-quality mathematics program for each and every student.</p> <ul style="list-style-type: none"> <li>• <b>2006 Curriculum Focal Points</b></li> </ul> <p>Curriculum Focal Points are the most important mathematical topics for each grade level. They comprise related ideas, concepts, skills, and procedures that form the foundation for understanding and using mathematics and lasting learning. Curriculum Focal Points have been integral in the revision of many state math standards for Pre-K through grade 8.</p> <ul style="list-style-type: none"> <li>• <b>2010 Focus in High School Mathematics</b></li> </ul> <p>Focus in High School Mathematics: Reasoning and Sense Making is a conceptual framework to guide the development of future publications and tools related to grades 9–12 mathematics curriculum and instruction. It suggests practical changes to the high school mathematics curriculum to refocus learning on reasoning and sense making. This shift constitutes a substantial rethinking of the high school math curriculum, advocating for more and better mathematics.</p>
Slide 4	<p>Source: NCTM <i>Principles to Actions</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)</p> <p>Continuing its tradition of mathematics education leadership, NCTM has defined and described the principles and actions, including specific teaching practices, that are essential for a high-quality mathematics education for all students.</p>
Slide 5	<p>The development of the standards began with research-based learning progressions detailing what is known today about how students’ mathematical knowledge, skill, and understanding develop over time. The knowledge and skills students need to be prepared for mathematics in college, career, and life are woven throughout the mathematics standards. However, the Standards do not describe or prescribe the teacher practices or actions that will ensure all students will be successful and mathematically literate.</p>

<p>Slide 6</p>	<p>Standards have contributed to higher achievement, but challenges remain.</p> <ul style="list-style-type: none"> <li>• In 2019, the National Assessment of Educational Progress (NAEP) mathematics assessment was administered to representative samples of fourth- and eighth-grade students in the nation, states, the District of Columbia, Department of Defense schools, and 27 participating large urban districts. The assessment was delivered on digital devices and assessed students' knowledge and skills in mathematics and their ability to solve problems in mathematical and real-world contexts. Students also answered survey questions asking about their opportunities to learn about and engage in mathematics inside and outside of school.</li> <li>• Mathematical performance, for PISA, measures the mathematical literacy of a 15-year-old student to formulate, employ and interpret mathematics in a variety of contexts to describe, predict and explain phenomena, recognizing the role that mathematics plays in the world. The mean score is the measure. A mathematically literate student recognizes the role that mathematics plays in the world in order to make well-founded judgments and decisions needed by constructive, engaged and reflective citizens.</li> <li>• 2019 NAEP: Lower-, middle-, and higher-performing students at grades 4 and 8 made gains compared to the early 1990s and 2000; <b>no significant progress was made at both grades for lower-performing students compared to a decade ago.</b></li> </ul>
<p>Slide 7</p>	<p>Source: NCTM <i>Principles to Actions</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)  Source: NCTM (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)  Summarize the Teaching and Learning Principle, noting the strong emphasis on promoting students' ability to make sense of mathematical ideas and to reason mathematically. Ask the participants to keep this Principle in mind throughout the session and in particular, as they watch the WV Classroom Video.</p>
<p>Slide 8</p>	<p><b>Prior to the workshop</b> and based on the expected number of participants, prepare packets of the Beliefs About Teaching and Learning Mathematics cards. Cut the cards apart, shuffle the cards and place them in an envelope. Each pair or group of participants will need one packet of cards. Also, prepare a packet of cards for you to use during the discussion of the activity.</p>

	<p>During the activity, circulate among the pairs or groups of participants as they work to sort the belief cards.</p> <p>After all pairs or groups have completed the sorting task, ask the participants if there were any belief cards they found difficult to classify as either Productive or Unproductive. Ask why they found it difficult to assign the belief card to a category.</p> <p>Select a belief card from your packet and read the card to the participants. Ask the participants how they classified the belief and why. Repeat selecting cards and engaging the participants until 3 to 5 cards have been discussed. Be sure to select both Productive and Unproductive beliefs.</p> <p>At the end of the discussion, move to the next slide so that participants may see the correct sorting.</p> <p>Source: <i>Principles to Actions, Ensuring Mathematical Success for All</i>, (NCTM, 2014) pg. 11.</p>
Slide 9	<p>Source: <i>Principles to Actions, Ensuring Mathematical Success for All</i>, (NCTM, 2014) pg. 11.</p>
Slide 10	<p>Source: NCTM <i>Principles to Action</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)</p>
Slide 11	<p>Source: NCTM <i>Principles to Actions</i> (<a href="http://www.nctm.org/principlestoactions">www.nctm.org/principlestoactions</a>)</p> <p>These are the practices at the heart of the work of teaching. According to the research of D. Ball and F.M. Forzani they are the practices that are most likely to affect student learning. Give participants a few minutes to review the list of the eight, research-based, Mathematics Teaching Practices identified by NCTM as highly effective for student learning of mathematics.</p> <p>Ask the participants to identify the most significant noun within each of the eight practices.</p> <ol style="list-style-type: none"> <li>1. Establish mathematics <b>goals</b> to focus learning.</li> <li>2. Implement <b>tasks</b> that promote reasoning and problem solving.</li> <li>3. Use and connect mathematical <b>representations</b></li> <li>4. Facilitate meaningful mathematical <b>discourse</b>.</li> <li>5. Pose purposeful <b>questions</b>.</li> <li>6. Build procedural <b>fluency</b> from conceptual understanding.</li> <li>7. Support productive <b>struggle</b> in learning mathematics.</li> <li>8. Elicit and use <b>evidence</b> of student thinking.</li> </ol>

Slide 12	<p>Source: Creating a Road Map, Corwin Publishing  <a href="https://us.corwin.com/sites/default/files/upm-binaries/92312_Chapter_2_Implementing_Effective_Teaching.pdf">https://us.corwin.com/sites/default/files/upm-binaries/92312_Chapter_2_Implementing_Effective_Teaching.pdf</a></p> <p>Give each participant the handout, Effective Teaching Look Fors.  Discuss the “Look Fors” for each Teaching Practice. Make sure all participants have the same understanding of what each “Look For” as they will be using this “Look Fors” later in the presentation to evaluate teaching methods.</p>
Slide 13	<p>Explain to the participants that they are about to view a video featuring a WV teacher and her students.</p> <p>Fitting Boxes Into Boxes is a series of culminating activities where the students work in groups to reach a solution. The students use what they have learned to determine the most economical way to ship jewelry boxes using the United States Postal Service (USPS) flat-rate options. In Part 1, students make sense of the task, outline what they will need to know and do to answer the question and map out their plan. In Part 2, they model the problem, calculate the number of jewelry boxes that will fit into each shipping box, and determine the associated costs. Students experiment with different orientations for the jewelry boxes to optimize space and minimize cost. In Part 3, they reflect, and discuss in the group and prepare to present. Students explain their strategies, reasoning, and evaluate the decisions about how to fit all 270 jewelry boxes so they ship at the lowest cost . In the culminating part of this activity, the groups report to the class about their solution, different arrangements of the jewelry boxes and the size of the shipping boxes that affected the unit cost for shipping each box of jewelry.</p>
Slide 14	
Slide 15	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 12.</p> <p>One of the research-based, teaching practices identified by NCTM is the importance of establishing clear mathematics goals to focus student learning and to guide teacher decisions. The mathematical purpose of a lesson should not be a mystery to students. Classrooms in which students understand the learning expectations for their work perform at higher levels than classrooms where the expectations are unclear (Haystead and Marzano 2009; Hattie</p>

	<p>2009). Although daily goals need not be posted, it is important that students understand the mathematical purpose of a lesson and how the activities contribute to and support their mathematics learning. Goals or essential questions motivate learning when students perceive the goals as challenging but attainable (Marzano 2003; McTighe and Wiggins 2013). Teachers can discuss student-friendly versions of the mathematics goals as appropriate during the lesson so that students see value in and understand the purpose of their work (Black and William 1998a; Marzano 2009). When teachers refer to the goals during instruction, students become more focused and better able to perform self-assessment and monitor their own learning (Clarke, Timperley, and Hattie 2004; Zimmerman 2001).</p>
Slide 16	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 12.</p>
Slide 17	<p>Source: YouTube  <a href="https://www.youtube.com/watch?v=EcZBUFqFLxc">https://www.youtube.com/watch?v=EcZBUFqFLxc</a></p>
Slide 18	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 16.</p> <p>Compare the actions of teachers versus the actions of students when establishing mathematics goals to focus learning.</p> <p>Ask the participants if they believe the teacher actions above are routine in their schools. If yes, ask how they know. If no, ask what is needed for the teacher actions above to become routine in their school.</p>
Slide 19	<p>The WV College and Career Readiness Standards (WVCCR) in this lesson refers to the students' ability to understand and use quotients of fractions in the real-world setting.</p> <p>The teacher might use an "I Can" statement for the student to understand the focus.</p> <p>"I can use multiplication and division of fractions to reason about real-world volume problems."</p> <p>The second WVCCR standard refers to the ability of finding the volume of a right rectangular prism with fractional edge lengths.</p>

<p>Slide 20</p>	<p>The learning goals of this lesson could be written in student friendly language. The students need to understand what they are learning. The first goal of “explain the strategies and reasoning of their solution” would be ‘Tell us how you find your answer and why you chose this method.’ The second learning goal would be “ judge your decision about how to fit all 270 jewelry boxes so they will be shipped at the lowest cost.” The third one could be stated as “compare the different ways jewelry boxes could be packed inside a larger shipping box. Tell us how each arrangement is different.” The fourth goal might be “identity the known information and decide what information is needed to solve this problem about the shipping costs.” Learning goals need to be have clear verbs, small and specific, in a checklist sequence that will give students the needed boost to feel successful.</p>
<p>Slide 21</p>	<p>The introduction of the lesson is one of the most crucial parts to engage the students in the math learning time. In this video clip of the lesson, Fitting Boxes into Boxes, Rachel Moon, the sixth grade teacher at John Adams Middle School, is stating the problem with her class. She has arranged the students in groups of three or four. The PowerPoint with the lesson’s task is projected for the students. Her introduction of the inquiry-based math problem is sparking the students’ critical thinking skills while using a real-world connection. You will see how the teacher, Rachel Moon, focuses the students to make sense of the task, outline what additional information they need to know and do in order to answer the question and map out their plan of action.</p> <p>Show Video clip</p> <p>Other options to spark students’ interest and engage their critical thinking might be visual clip of the United States Postal Service such as <a href="https://youtu.be/U3g9ekGHxBs">https://youtu.be/U3g9ekGHxBs</a> or an audio song like Mr. Postman by Beatles (play to 2:18) to spark thinking. (<a href="https://youtu.be/Jzy4R8EbWJ4">https://youtu.be/Jzy4R8EbWJ4</a> Beatles Song Mr. Postman)</p> <p>THINK, PAIR AND SHARE</p> <p>Ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p> <p>Bring the group back together to summarize their thoughts.</p> <p>Fitting Boxes into Boxes Math’s Expectations::</p>

1. Students will apply the understandings in computing the volume of right rectangular prisms, including those with fractional edge lengths. Students utilize the formulas of length x width x height and area of base x height to determine the volume.
2. Students' familiarity with the commutative property of multiplication allows them to comprehend that, regardless of how the box lies, its volume remains the same.
3. Students' developed skills and understandings about a variety of methods to compute the quotient of fractions through a variety of methods, including tape diagrams and the standard algorithm will be utilized in the problem. Students will think about the different ways they have used fractions in calculations.
4. Students will think of a strategy for considering different configurations efficiently,
5. Students will test out different arrangements and how they affect the number of jewelry boxes to be fitted and the cost.
6. Students will calculate the cost of shipping jewelry boxes in each of the USPS flat-rate boxes.

In what ways did the math goals focus the teacher's interactions with the students throughout the lesson?

The key to making these students' learning experience worthwhile is to focus the planning and interactions on math expectations and goals or phrased in terms of desired student outcomes—the knowledge, skills, attitudes, values, and mathematical dispositions that the teacher wants to develop in the students.

In this learning problem, the teacher's interactions are aimed to providing feedback specific to math expectations and goals. The teacher's feedback and open-ended questions as he/she walks around and checks on the groups' progress helps her students improve their performance and solidify their understanding.

The math expectations, learning goals and providing feedback work in tandem. As the students work in groups, the teacher is listening, checking to see if progress is being made, and providing thought provoking comments to redirect any groups who are frustrated beyond productive math struggle. Providing feedback is an ongoing process for the teacher and as she monitors, the students are continually working toward the math goals. The teacher, Rachel Moon, assists by communicating in the interactions to the students prompts . She provides thought-provoking comments that helps them better

	<p>understand what they are to learn and what changes are necessary to improve their learning or completion of this math problem. One point you will notice is as the teacher she does not give the students the answers.</p>
Slide 22	
Slide 23	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 17.</p> <p>There is <b>no decision that teachers make that has a greater impact on students' opportunities to learn and on their perceptions about what mathematics is than the selection or creation of the tasks</b> with which the teacher engages students in studying mathematics.</p> <p>Tasks should provide opportunities for students to think and make sense of mathematics.</p> <p>Having <b>multiple entry points is very important</b> because of the <b>impact on equity</b>. If students can make a table, create a drawing, or use manipulatives, the math becomes more accessible to students who might not immediately know how to solve the problem.</p>
Slide 24	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 17.</p> <p>Tasks should provide opportunities for students to make sense of mathematics. Rich mathematical tasks engage students in sense-making through deeper learning that require high levels of thinking, reasoning, and problem solving.</p>
Slide 25	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p. 18.</p> <p>THINK, PAIR AND SHARE:</p> <p>Ask participants if the math tasks provided in students' texts have all the characteristics of a GOOD math task. If NO, discuss what traits are usually missing in textbook provided math tasks.</p> <p>Ask participants to share how they find GOOD math tasks (outside of the adopted textbook) for their students.</p>

Slide 26	<p>Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving such as this learning activity. Effective teaching with this kind of mathematical problem engages students in solving and discussing real world applications of the math concepts. In this video, Rachel Moon, the teacher is encouraging the students to reason and promote their higher-level thinking in the group.</p> <p>Video clip: THINK, PAIR AND SHARE</p> <p>Ask participants to respond to the question. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form. Give the participants time to communicate and discussion this question.</p> <p>Sample responses might include: There were multiple entry points in this task due to the fact the teacher did not tell the students you need to solve this problem by following specific steps. The students had to discussion, think, and reason how to find a solution. The problem or tasks did not have one way to solve it. The students could have different arrangement of jewelry box in the different sizes of shipping boxes which would lead to a variety of outcomes. Often there will be a gap left where additional jewelry boxes will fit. Each mailing box allows for several different arrangements. For example, the small shipping box: had almost 18 (3 by 3 by 2) jewelry boxes can fit into the shipping box (other arrangements would lead to fewer boxes).</p>
Slide 27	
Slide 28	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 24</p> <p>Ask participants what is meant by representations of mathematical ideas.</p>
Slide 29	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 24</p>
Slide 30	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 25</p>

	<p>Engage participants in a discussion of the graphic. Some probing questions you might ask include:</p> <ul style="list-style-type: none"> <li>• What is the distinction between physical and visual representations? <ul style="list-style-type: none"> <li>• Describe some physical representations that might support students' thinking.</li> <li>• Describe some visual representations you would expect students to produce.</li> <li>• In the diagram, why do the arrows go both ways?</li> </ul> </li> </ul> <p>The point is not for students to use different representations just for the sake of it. What's crucial is that students are using/connecting representations as TOOLS to solve problems and to build understanding of concepts. The depth of understanding is related to the strength of connections among mathematical representations that students have internalized (Pape and Tchoshanov 2001; Webb, Boswinkel, and Dekker 2008). For example, students develop understanding of the meaning of the fraction <math>\frac{7}{4}</math> (symbolic form) when they can see it as the quantity formed by "7 parts of size one-fourth" with a tape diagram or on a number line (visual form), or measure a string that has a length of 7-fourths yards (physical form).</p>
Slide 31	Source: <i>Principles to Action: Ensuring Mathematical Success for All</i> , NCTM, 2014, p. 25
Slide 32	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources  <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a></p> <p>Provide participants with a copy of the Rich Mathematical Task Rubric. Allow time for participants to read the rubric.</p> <p>Discuss the Task Levels and the Descriptions for <b>Representations and Connections</b>.</p>
Slide 33	<p>In this video clip, you will see a young student solving the problem of how many jewelry boxes would fit by using pictures and drawings.</p> <p>Video clip</p> <p>Lead a discussion about how the student is connecting the math concepts of finding volume with this representational approach.</p> <p>THINK, PAIR AND SHARE</p>

	In pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.
Slide 34	
Slide 35	Source: Principles to Action: Ensuring Mathematical Success for All, NCTM, 2014, p. 29 Ask participants what their concerns are about facilitating meaningful mathematical discourse.
Slide 36	Source: <i>Asking Questions and Promoting Discourse</i> , NCTM <a href="https://www.nctm.org/Conferences-and-Professional-Development/Tips-for-Teachers/Asking-Questions-and-Promoting-Discourse/">https://www.nctm.org/Conferences-and-Professional-Development/Tips-for-Teachers/Asking-Questions-and-Promoting-Discourse/</a> Mathematical discourse is a powerful sense-making tool, but it doesn't just <i>happen</i> . Students must develop both the inclination and habit of attending to each other's mathematical ideas, and they must have the time and space to make sense of, critique, and develop the ideas. Teacher talk moves are crucial supports for developing students' capacity to engage in productive mathematical discussions (Kazemi and Hintz, 2014; Chapin, O'Connor, and Anderson, 2009).
Slide 37	Source: Principles to Action: Ensuring Mathematical Success for All, NCTM , 2014, p.35. Ask participants about student interest in engaging in mathematical discourse. Why do some students try to avoid participating in mathematical discourse? How can the teacher help students to become more active participants in mathematical discourse?
Slide 38	Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources Grades 6-8 Institute PowerPoint <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a> The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive

	<p>1.20. The higher the score, the greater the positive impact of the action on student achievement.</p> <p>Classroom discussion has an effect size of 0.82, which is more than twice what we need to know that a specific strategy will make a difference in learning. Classroom discussion is defined as “a method of teaching that involves the entire class in a discussion.</p> <p>Classroom discussion is a critical area with a huge effect size. Classroom discussions provide the opportunity for students to communicate with one another for a variety of functions including to activate prior knowledge, to explore new topics, to learn from others, and to demonstrate their learning. This is an engagement strategy which provides all students the chance to participate, especially when structured in a way that extends beyond a teacher-student question and answer sequence.</p> <p>Consider what <a href="http://visiblelearning.org">visiblelearning.org</a>, asserts regarding what the most effective classrooms discussions should include:</p> <ul style="list-style-type: none"> <li>• creating a series of questions for the students to think about</li> <li>• allocating enough time in the lesson for an elaborate discussion</li> <li>• making sure that students can freely express their opinion without being laughed at or ridiculed</li> </ul>
Slide 39	<p>There is no clip for this slide.</p> <p>THINK, PAIR AND SHARE</p> <p>In pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 40	
Slide 41	<p>Ask participants how posing purposeful questions can be used to inform instruction and assess student understanding?</p> <p>Ask participants how posing purposeful questions can promote equitable learning opportunities for all students?</p> <p><b>Identify, in advance, the big ideas that your lesson examines and the mathematical outcomes that students should achieve.</b> Take time to brainstorm the multiple approaches that could be taken to work through similar problems and the misconceptions that students might have. Make sure that you prepare questions that address these multiple approaches and</p>

	<p>misconceptions, prompting a discussion about when particular approaches are better than others and how to explain why each misconception is faulty. Close each lesson with a summarizing question that reiterates the big ideas.</p>
Slide 42	<p>Source: Principles to Action: Ensuring Mathematical Success for All, NCTM, 2014</p> <p>Effective mathematics teaching relies on questions that encourage students to explain and reflect on their thinking as an essential component of meaningful mathematical discourse. Purposeful questions allow teachers to discern what students know and adapt lessons to meet varied levels of understanding, help students make important mathematical connections, and support students in posing their own questions. However, merely asking questions is not enough to ensure that students make sense of mathematics and advance their reasoning.</p>
Slide 43	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources Grades 6-8 Institute PowerPoint <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a></p> <p>The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement.</p> <p>Ask participants why Self-verbalization and Self-questioning have a greater impact on student achievement.</p> <p>So much of classroom time is spent with teachers questioning the students. Cotton (1989), for example, reviewed the evidence and found questioning was the second most dominant teaching method (after teacher talk), with teachers spending between 35–50 percent of teaching time posing questioning (e.g., Long &amp; Sato, 1983; van Lier, 1998)— that is about 100 questions per hour (Mohr, 1998)—and the responses from the teacher to the students’ answers to these questions was some form of judgment or correction, primarily reinforcing in nature, affirming, restating, and consolidating student responses. Brualdi (1998) claimed that teachers asked 300 to 400 questions per day, and</p>

	<p>the majority of these were low-level cognitive questions—60 percent recall facts and 20 percent are procedural in nature (Wilén, 1991) These are not open, inquiry questions, as students understand that the teacher already knows the answer (they are “display” questions; 82 percent are of this nature: Cotton, 1989). The reason for so much questioning relates to the conceptions of teaching and learning held by many teachers—that is, their role is to impart knowledge and information about a subject, and student learning is the acquisition of this information through processes of repetition, memorization, and recall: hence the need for much questioning to check that they have recalled this information. The overall effects of questioning vary, and the major moderator is the type of question asked—surface questions can enhance surface knowing and higher-order questions can enhance deeper understanding.</p>
<p>Slide 44</p>	<p>Adapted from Smith, M. S., et al. (2017). <i>Taking Action: Implementing Effective Mathematics Teaching Practices</i>, National Council of Teachers of Mathematics, p.102</p> <p>Researchers have created a variety of frameworks to categorize the types of questions that teachers ask (e.g., Boaler and Brodie 2004; Chapin and O’Connor 2007). Though the categories differ across frameworks, commonalities exist among the types of questions. For example, the frameworks generally include questions that ask students to recall information, as well as questions that ask students to explain their reasoning. The chart above displays a set of question types that synthesizes key aspects of these frameworks that are particularly important for mathematics teaching. Although the question types differ with respect to the level of thinking required in a response, all of the question types are necessary in the interactions among teachers and students. For example, questions that gather information are needed to establish what students know, while questions that encourage reflection and justification are essential to reveal student reasoning.</p>
<p>Slide 45</p>	<p>Points or comments that might be forthcoming from the audience:</p> <ol style="list-style-type: none"> <li>1. The teacher, Rachel Moon, was crafting <i>questions</i> that help <i>students</i> deepen their <i>thinking</i> rather telling the students what to do.</li> </ol>

	<p>2. You will notice her comments with <i>questions</i> are on the video is guiding the students to the right track: Posing <i>purposeful questions</i> is necessary to keep students working productively.</p> <p>3. Rachel Moon used questions like these in the video. You might want a few general questions in your "back pocket" to <u>guide students</u> stumped by <u>any math problem</u>.</p> <p>4. Teachers (in the clip :Rachel Moon) can also support productive struggle by <i>asking questions</i> that make student think about they are doing or solving.</p> <p>Here are some purposeful questions you want to keep handy to use with any math problem:</p> <ul style="list-style-type: none"> <li>• What do you already know? What do you need to know?</li> <li>• What do you understand so far?</li> <li>• What parts of this problem make sense to you?</li> <li>• What in this problem doesn't yet make sense to you?</li> <li>• How might we decide which approach makes more sense?</li> <li>• What are some math ideas we've worked on before that could help you with this new idea?</li> </ul> <p>THINK, PAIR AND SHARE</p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 46	
Slide 47	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014</p> <p>Ask participants to share their thoughts on the importance of fluency with procedures to student success in mathematics.</p> <p>Discuss with the participants the significance of the quote: <i>A rush to fluency undermines students' confidence and interest in mathematics and is considered a cause of mathematics anxiety.</i></p>
Slide 48	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014</p> <p>Paraphrase the bullets on the slide.</p>

	<p>Fluency is not intended as the main or sole target of instruction. Problem Solving and Reasoning that are the focus of the second teaching practice need to co-exist with procedural fluency. This occurs when students first have opportunities to develop conceptual understanding.</p> <p>Computational fluency is strongly related to number sense and involves so much more than the conventional view of it encompasses. Developing students' computational fluency extends far beyond having students memorize facts or a series of steps unconnected to understanding (Baroody 2006; Griffin 2005)</p> <p>Early work with reasoning strategies is related to algebraic reasoning. As students learn how quantities can be taken apart and put back together in different ways (i.e., decomposition and composition of numbers), they establish a basis for understanding properties of the operations. Students need this early foundation for meaningful learning of more formal algebraic concepts and procedures throughout elementary school and into middle and high school.</p>
Slide 49	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 42.</p> <p>Discuss why is it important to build procedures from conceptual understanding.</p> <p>Ask participants: What kind of “bizarre results’ could happen if students are taught mechanical execution of procedures without understanding the mathematical basis?</p> <p>Fluency is not a simple idea. Being fluent means that students are able to choose flexibly among methods and strategies to solve contextual and mathematical problems, they understand and are able to explain their approaches, and they are able to produce accurate answers efficiently. Fluency builds from initial exploration and discussion of number concepts to using informal reasoning strategies based on meanings and properties of the operations to the eventual use of general methods as tools in solving problems. This sequence is beneficial whether students are building toward fluency with single- and multi-digit computation with whole numbers or fluency with, for example, fraction operations, proportional relationships, measurement formulas, or algebraic procedures.</p>

Slide 50	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 47</p> <p>Ask participants:</p> <p>What visual models have they used to build procedural fluency?</p> <p>Is it important for students to be able to explain why the procedures they used worked? Why?</p>
Slide 51	<p>Video clip</p> <p>In this video clip, you see Rachel Moon building procedural fluency and making sure the students understand they are working on the volume of the boxes. In this type of math problem, the teacher, Rachel Moon is providing students with opportunities to use their own reasoning strategies and methods for solving problems</p> <p>She is asking students to discuss and explain why the procedures that they are using work to solve particular problems.</p> <p>In as you see in the video, the teacher is discussing about connecting student-generated strategies and methods to more efficient procedures as appropriate.</p> <p>Rachel Moon used visual model of the shipping box to support students' understanding of general methods of finding volume versus finding surface area.</p> <p>Overall, this math activity provides students with opportunities use of the procedural practices.</p> <p>THINK, PAIR AND SHARE</p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
Slide 52	
Slide 53	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014</p> <p>Discuss with the participants the importance for students to be able to figure things out for themselves.</p> <p>It is through this process of figuring things out on their own that they will develop authority and ownership of their own learning.</p>

<p>Slide 54</p>	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p.48.</p> <p>In comparisons of mathematics teaching in the United States and in high-achieving countries, U.S. mathematics instruction has been characterized as rarely asking students to think and reason with or about mathematical ideas (Banilower et al. 2006; Hiebert and Stigler 2004). Teachers sometimes perceive student frustration or lack of immediate success as indicators that they have somehow failed their students. As a result, they jump in to “rescue” students by breaking down the task and guiding students step by step through the difficulties. Although well intentioned, such “rescuing” undermines the efforts of students, lowers the cognitive demand of the task, and deprives students of opportunities to engage fully in making sense of the mathematics.</p>
<p>Slide 55</p>	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources Grades 6-8 Institute PowerPoint <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a></p> <p>The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement.</p> <p>There is a high relationship between engagement and degree of concentration on tasks. One way of enhancing concentration is to mentally visualize the processes and strategies involved in a task. Students who mentally visualized various motor tasks were more effective compared to those that did not (<math>d = 0.48</math>).</p> <p>Teachers greatly influence how students perceive and approach struggle in the mathematics classroom. Even young students can learn to value struggle as an expected and natural part of learning, as demonstrated by the class motto of one first-grade math class: “If you are not struggling, you are not learning” (Carter 2008, p. 136). Teachers must accept that struggle is important to students’ learning of mathematics, convey this message to students, and provide time for them to try to work through their uncertainties.</p> <p>Unfortunately, this may not be enough, since some students will still simply shut down in the face of frustration, proclaim “I don’t know,” and give up.</p>

	<p>Dweck (2006) has shown that students with a fixed mindset— that is, those who believe that intelligence (especially math ability) is an innate trait—are more likely to give up when they encounter difficulties because they believe that learning mathematics should come naturally. By contrast, students with a growth mindset—that is, those who believe that intelligence can be developed through effort—are likely to persevere through a struggle because they see challenging work as an opportunity to learn and grow.</p>
<p>Slide 56</p>	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p.52.</p> <p>Use the chart to engage participants in a discussion of how they support students to persevere in problem solving.</p>
<p>Slide 57</p>	<p>In this clip, you will see Rachel Moon working with one of the math groups as they have been struggling. As she was walking around the classroom and monitoring the learning in each group, she stop to discuss with these three students about their direction of solving the problem.</p> <p>Video clip</p> <p>What did you notice in the clip?</p> <p>Rachel Moon is teaching that struggling is part of learning math. She wants to encourage creativity and build authentic engagement and perseverance in her students. She guiding their thoughts with the direction that the solution is going to make sense. Here students are encouraged to seek solutions that are grounded in logic, prior knowledge and that make sense to them, instead of imitating methods used by other students. Faced with this challenge, these students are experiencing the discomfort of not knowing. However, especially with practice and working together, they become more comfortable with enduring this tension and working through it. Eventually, these will also experience the incredible personal satisfaction of solving a challenging problem.</p> <p>THINK, PAIR AND SHARE</p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>

Slide 58	
Slide 59	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 53</p> <p>Ask participants:</p> <p>What can serve as evidence of student thinking when assessing progress toward understanding?</p> <p>How should the evidence affect what a teacher does instructionally for students?</p>
Slide 60	<p>Source: <i>Principles to Action: Ensuring Mathematical Success for All</i>, NCTM, 2014, p. 53</p> <p>Ask participants:</p> <p>What is formative assessment?</p> <p>Is it possible to do formative assessment every day?</p> <p>If so, how?</p>
Slide 61	<p>Source: Virginia Department of Education Mathematics Institutes 2019 Professional Development Resources  Grades 6-8 Institute PowerPoint  <a href="http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml">http://www.doe.virginia.gov/instruction/mathematics/professional_development/institutes/2019/index.shtml</a></p> <p>The chart is from the work of Dr. John Hattie. He analyzed the impact of student, teacher, home, curriculum and community actions on student learning. Based on data, each action scored an Effect Rate for the ability to affect student achievement. The values range from a negative .20 to a positive 1.20. The higher the score, the greater the positive impact of the action on student achievement.</p> <p>Cognitive task analysis was among the highest scoring actions to affect student achievement.</p> <p>Ask participants to give an example of what a cognitive task might look like in the classroom and why it is so effective.</p>
Slide 62	<p>Set up: In this clip, you will see Rachel Moon eliciting and using evidence of the students' thinking in our math problem.</p> <p>Play: Video Clip</p> <p>Follow-up:</p>

	<p>What did you notice about the teacher’s conversation with the students? Rachel Moon, the teacher, was asking good questions (and at that right time) to generate the types of thinking and discussion that are central to the learning goals. She is listening carefully to student thinking and make note of which ideas to bring to the forefront of whole class discussions and the order to discuss those ideas relative to the learning goals. When you, the teacher, are eliciting and using evidence of student thinking, some questions you might use are: Who Disagrees? Who will explain why or why not? Who has the same answer, but a different way to explain it? Who has a different answer? You, the teacher, are listening carefully to students’ ideas and math problems such as Fitting Boxes into Boxes can provide you useful information about student thinking and areas you may need to reteach or provide individual instruction to certain students.</p> <p><b>THINK, PAIR AND SHARE</b></p> <p>With participants grouped in pairs, ask participants to respond to the questions. Remind them to utilize their completed <i>Effective Teaching Look Fors</i> form.</p>
<p>Slide 63</p>	<p><b>THINK, PAIR AND SHARE – CLOSURE ACTIVITY</b></p> <p>With participants grouped in pairs, ask participants to reflect on what they have learned about the eight Effective Mathematics Teaching Practices. Ask each participant to select 1-2 Practices to study and to implement with students.</p> <p>In pairs, develop a list of actions they will need to take in the pursuit of mathematical success for all their students.</p>
<p>Slide 64</p>	